

## Sample Problems – Chapter 10

Title: Cost of Debt

1. Costly Corporation plans a new issue of bonds with a par value of \$1,000, a maturity of 28 years, and an annual coupon rate of 16.0%. Flotation costs associated with a new debt issue would equal 9.0% of the market value of the bonds. Currently, the appropriate discount rate for bonds of firms similar to Costly is 17.0%. The firm's marginal tax rate is 30%. What will the firm's true cost of debt be for this new bond issue?

- a. 20.99%
- b. 18.69%
- c. 17.61%
- d. 12.32%
- e. 13.08%

Title: Cost of preferred stock

2. Costly Corporation is also considering using a new preferred stock issue. The preferred would have a par value of \$400 with an annual dividend equal to 18.0% of par. The company believes that the market value of the stock would be \$968.00 per share with flotation costs of \$68.00 per share. The firm's marginal tax rate is 40%. What would the firm's cost of preferred be for this new preferred stock issue?

- a. 8.00%
- b. 7.44%
- c. 8.79%
- d. 6.92%
- e. 6.28%

Title: Cost of internal equity (new dividend)

3. Costly Corporation is considering using equity financing. Currently, the firm's stock is selling for \$47.00 per share. The firm's dividend for next year is expected to be \$3.40 with an annual growth rate of 5.0% thereafter indefinitely. If the firm issues new stock, the flotation costs would equal 14.0% of the stock's market value. The firm's marginal tax rate is 40%. What is the firm's cost of internal equity?

- a. 11.53%
- b. 13.41%
- c. 12.60%
- d. 13.83%
- e. 12.23%

Title: Cost of external equity (new dividend)

4. Costly Corporation is considering using equity financing. Currently, the firm's stock is selling for \$31.00 per share. The firm's dividend for next year is expected to be \$5.50 with an annual growth rate of 5.0% thereafter indefinitely. If the firm issues new stock, the flotation costs would equal 15.0% of the stock's market value. The firm's marginal tax rate is 40%. What is the firm's cost of external equity?

- a. 23.63%
- b. 22.74%
- c. 25.87%
- d. 26.92%
- e. 24.39%

Title: WACC using RE (before-tax debt)

5. Marginal Incorporated (MI) has determined that its before-tax cost of debt is 9.0%. Its cost of preferred stock is 15.0%. Its cost of internal equity is 17.0%, and its cost of external equity is 19.0%. Currently, the firm's capital structure has \$378 million of debt, \$63 million of preferred stock, and \$459 million of common equity. The firm's marginal tax rate is 45%. The firm is currently making projections for next period. Its managers have determined that the firm should have \$92 million available from retained earnings for investment purposes next period. What is the firm's marginal cost of capital at a total investment level of \$155 million?

- a. 14.52%
- b. 12.82%
- c. 12.31%
- d. 11.80%
- e. 13.50%

Title: WACC using New stock (before-tax debt)

6. Marginal Incorporated (MI) has determined that its before-tax cost of debt is 9.0%. Its cost of preferred stock is 15.0%. Its cost of internal equity is 17.0%, and its cost of external equity is 19.0%. Currently, the firm's capital structure has \$378 million of debt, \$63 million of preferred stock, and \$459 million of common equity. The firm's marginal tax rate is 45%. The firm is currently making projections for next period. Its managers have determined that the firm should have \$92 million available from retained earnings for investment purposes next period. What is the firm's marginal cost of capital at a total investment level of \$247 million?

- a. 12.31%
- b. 11.80%
- c. 12.82%
- d. 14.52%
- e. 13.50%

Title: WACC using RE (after-tax debt)

7. Marginal Incorporated (MI) has determined that its after-tax cost of debt is 9.0%. Its cost of preferred stock is 15.0%. Its cost of internal equity is 17.0%, and its cost of external equity is 19.0%. Currently, the firm's capital structure has \$378 million of debt, \$63 million of preferred stock, and \$459 million of common equity. The firm's marginal tax rate is 45%. The firm is currently making projections for next period. Its managers have determined that the firm should have \$92 million available from retained earnings for investment purposes next period. What is the firm's marginal cost of capital at a total investment level of \$157 million?

- a. 13.50%
- b. 14.52%
- c. 14.01%
- d. 12.82%
- e. 11.80%

Title: WACC using New stock (after-tax debt)

8. Marginal Incorporated (MI) has determined that its after-tax cost of debt is 9.0%. Its cost of preferred stock is 15.0%. Its cost of internal equity is 17.0%, and its cost of external equity is 19.0%. Currently, the firm's capital structure has \$378 million of debt, \$63 million of preferred stock, and \$459 million of common equity. The firm's marginal tax rate is 45%. The firm is currently making projections for next period. Its managers have determined that the firm should have \$92 million available from retained earnings for investment purposes next period. What is the firm's marginal cost of capital at a total investment level of \$247 million?

- a. 14.52%
- b. 13.50%
- c. 14.01%
- d. 12.82%
- e. 11.80%

Title: WACC (before-tax cost of debt)

9. Marginal Incorporated (MI) has determined that its before-tax cost of debt is 7% for the first \$112 million in bonds it issues, and 8% for any bonds issued above \$112 million. Its cost of preferred stock is 10%. Its cost of internal equity is 14%, and its cost of external equity is 17%. Currently, the firm's capital structure has \$400 million of debt, \$100 million of preferred stock, and \$500 million of common equity. The firm's marginal tax rate is 30%. The firm is currently making projections for next period. Its managers have determined that the firm should have \$59 million available from retained earnings for investment purposes next period. What is the firm's marginal cost of capital at each of the following total investment levels?

- (A) Total investment level of \$380 million?
- (B) Total investment level of \$199 million?
- (C) Total investment level of \$69 million?

Title: WACC (after-tax cost of debt)

10. Marginal Incorporated (MI) has determined that its after-tax cost of debt is 6% for the first \$100 million in bonds it issues, and 8% for any bonds issued above \$100 million. Its cost of preferred stock is 9%. Its cost of internal equity is 12%, and its cost of external equity is 14%. Currently, the firm's capital structure has \$600 million of debt, \$100 million of preferred stock, and \$300 million of common equity. The firm's marginal tax rate is 30%. The firm is currently making projections for next period. Its managers have determined that the firm should have \$75 million available from retained earnings for investment purposes next period. What is the firm's marginal cost of capital at each of the following total investment levels?

- (A) Total investment level of \$280 million?
- (B) Total investment level of \$200 million?
- (C) Total investment level of \$77 million?

#### Answers:

- 1. e
- 2. a
- 3. e
- 4. c
- 5. d
- 6. c
- 7. a
- 8. a

1.

<b>N</b>	<b>I</b>	<b>***PV***</b>	<b>FV</b>	<b>PMT</b>
<b>28</b>	<b>17</b>	<b>941.90</b>	<b>1000</b>	<b>(0.16)(1000)</b>

<b>N</b>	<b>***I***</b>	<b>PV</b>	<b>FV</b>	<b>PMT</b>
<b>28</b>	<b>18.693</b>	<b>-[941.90 – (0.09)(941.90)]</b>	<b>1000</b>	<b>(0.16)(1000)</b>

After-tax cost of debt = (Before-tax cost of debt)(1 – marginal tax rate)

After-tax cost of debt = (18.693%)(1 – 0.30) = 13.08%

2.

N	***I***	PV	FV	PMT
1000	8	-(968 – 68)		(400)(0.18)

3.

$$k_s = \frac{D_1}{P_0} + g = \frac{3.40}{47} + 0.05 = 0.1223 = 12.23\%$$

4.

$$k_e = \frac{D_1}{P_0 - F} + g = \frac{5.50}{(31 - (0.15)(31))} + 0.05 = 0.2587 = 25.87\%$$

**For questions 5, 6, 7, and 8 start by calculating the capital structure weights and then calculate the retained earnings breakpoint.**

Capital Structure Weights

Debt	378	/	900	=	0.42
Pref	63	/	900	=	0.07
Eq	459	/	900	=	0.51
TOTAL	900				

Retained earnings breakpoint = (RE available)/(equity fraction) = (92 million)/(0.51) = 180.39 million

5. Use the cost of retained earnings for equity since the total investment level of \$155 million is less than the breakpoint for equity. Adjust for the tax effect for debt since the before-tax cost of debt is given.

$$WACC = (0.42)(9\%)(1 - 0.45) + (0.07)(15\%) + (0.51)(17\%) = 11.8\%$$

6. Use the cost of new stock for equity since the total investment level of \$247 million is greater than the breakpoint for equity. Adjust for the tax effect for debt since the before-tax cost of debt is given.

$$WACC = (0.42)(9\%)(1 - 0.45) + (0.07)(15\%) + (0.51)(19\%) = 12.82\%$$

7. Use the cost of retained earnings for equity since the total investment level of \$157 million is less than the breakpoint for equity. Do not adjust for the tax effect for debt since the after-tax cost of debt is given.

$$WACC = (0.42)(9\%) + (0.07)(15\%) + (0.51)(17\%) = 13.50\%$$

8. Use the cost of new stock for equity since the total investment level of \$247 million is greater than the breakpoint for equity. Do not adjust for the tax effect for debt since the after-tax cost of debt is given.

$$WACC = (0.42)(9\%) + (0.07)(15\%) + (0.51)(19\%) = 14.52\%$$

9.

**First, calculate the capital structure weights.**

Capital Structure Weights

Debt	400	/	1000	=	0.4
Pref	100	/	1000	=	0.1
Eq	500	/	1000	=	0.5
TOTAL	1000				

**Next, calculate the breakpoints. (There are two breakpoints in this problem since the cost of debt can be either 7% or 8% and the cost of equity can be 14% or 17%.)**

$$\text{Breakpoint(debt)} = 112/0.4 = 280 \text{ million}$$

$$\text{Breakpoint(equity)} = 59/0.5 = 118 \text{ million}$$

**Now calculate the WACC for each total investment level. You must adjust the cost of debt for taxes since you are given the before-tax cost of debt.**

A)

\$380 million total investment level

The total investment level exceeds the breakpoint for debt ( $380 > 280$ ), so you use the higher cost of debt.

The total investment level exceeds the breakpoint for equity ( $380 > 118$ ), so you use the higher cost of equity.

$$\text{WACC} = (0.4)(8\%)(1 - 0.30) + (0.1)(10\%) + (0.5)(17\%) = 11.74\%$$

B)

\$199 million total investment level

The total investment level is less than the breakpoint for debt ( $199 < 280$ ), so you use the lower cost of debt.

The total investment level exceeds the breakpoint for equity ( $199 > 118$ ), so you use the higher cost of equity.

$$\text{WACC} = (0.4)(7\%)(1 - 0.30) + (0.1)(10\%) + (0.5)(17\%) = 11.46\%$$

C)

\$69 million total investment level

The total investment level is less than the breakpoint for debt ( $69 < 280$ ), so you use the lower cost of debt.

The total investment level is less than the breakpoint for equity ( $69 < 118$ ), so you use the lower cost of equity.

$$\text{WACC} = (0.4)(7\%)(1 - 0.30) + (0.1)(10\%) + (0.5)(14\%) = 9.96\%$$

10.

**First, calculate the capital structure weights.**

Capital Structure Weights

Debt	600	/	1000	=	0.6
Pref	100	/	1000	=	0.1
Eq	300	/	1000	=	0.3
TOTAL	1000				

**Next, calculate the breakpoints. (There are two breakpoints in this problem since the cost of debt can be either 6% or 8% and the cost of equity can be 12% or 14%.)**

$$\text{Breakpoint(debt)} = 100/0.6 = 167 \text{ million}$$

$$\text{Breakpoint(equity)} = 75/0.3 = 250 \text{ million}$$

**Now calculate the WACC for each total investment level. You do not adjust the cost of debt for taxes since you are given the after-tax cost of debt.**

A)

\$280 million total investment level

The total investment level exceeds the breakpoint for debt ( $280 > 167$ ), so you use the higher cost of debt.

The total investment level exceeds the breakpoint for equity ( $280 > 250$ ), so you use the higher cost of equity.

$$\text{WACC} = (0.6)(8\%) + (0.1)(9\%) + (0.3)(14\%) = 9.90\%$$

B)

\$200 million total investment level

The total investment level exceeds the breakpoint for debt ( $200 > 167$ ), so you use the higher cost of debt.

The total investment level is less than the breakpoint for equity ( $200 < 250$ ), so you use the lower cost of equity.

$$\text{WACC} = (0.6)(8\%) + (0.1)(9\%) + (0.3)(12\%) = 9.30\%$$

C)

\$77 million total investment level

The total investment level is less than the breakpoint for debt ( $77 < 167$ ), so you use the lower cost of debt.

The total investment level is less than the breakpoint for equity ( $77 < 250$ ), so you use the lower cost of equity.

$$\text{WACC} = (0.6)(6\%) + (0.1)(9\%) + (0.3)(12\%) = 8.10\%$$